

On the generalizability of Pāṇini's *pratyāhāra*-technique to other languages

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अइउण्। ऋत्क्। एओङ्। ऐऔच्। हयवरट्।
लण्। अमडुणनम्। झमञ्। घढधष्। जबगडदश्।
खफछठथचटतव्। कपय्। शषसर्। हल्।

Pāṇini's Śivasūtras

1.	a	i	u			N	अइउण्। ऋल्क्। a.i.uɳ r.lk
2.				r	!	K	एओङ्। ऐऔच्। e.oɳ ai.auc
3.		e	o			Ṅ	
4.		ai	au			C	
5.	h	y	v	r		T	हयवरट्। लण्। hayavarat lan
6.					I	N	
7.	ñ	m	ń	ɳ	n	M	नमडंणनम्। झ्नभञ्। ñamanaṇanam jhabhañ
8.	jh	bh				Ṅ	
9.			gh	ɖh	dh	S	घढधष्। जबगडदश्। ghadhadhas jabagadadas
10.	j	b	g	ɖ	d	Ś	
11.	kh	ph	ch	ʈh	th	V	खफछठथचटतव्। khaphachathathacatatav
12.	k	p		c	t	Y	
13.			ś	ʂ	s	R	कपय्। शषसर्। हल्। kapay śasasar hal
14.	h					L	

Pāṇini's Śivasūtras

1.	a	i	u		N
2.				r	!
3.	e	o			Ṅ
4.	ai	au			C
5.	h	y	v	r	T
6.				I	N
7.	ñ	m	ń	ṇ	n
8.	jh	bh			Ṅ
9.			gh	ɖh	d̪h
10.	j	b	g	ɖ	d
11.	kh	ph	ch	ʈh	th
			c	ʈ	t
12.	k	p			Y
13.			ś	ʂ	s
14.	h				L

अइउण्। ऋत्तक्।
a·i·uɳ | r̪·lk |

एओङ्। ऐऔच्।
e·oɳ | ai·auc |

हयवरट्। लण्।
hayavarat | lan |

ऋमठणनम्। झ्वभञ्।
ñamanaṇanam | jhabhañ |

घढधष्। जबगडदश्।
ghadhadhas | jabagadadasá |

खफछठथचटतव्।
khaphachathathacatatav |

कपय्। शषसर्। हल्।
kapay | śaṣasar | hal |

Pāṇini's Śivasūtras

1.	a	i	u			N
2.				r	!	K
3.		e	o			Ṅ
4.		ai	au			C
5.	h	y	v	r		T
6.					I	N
7.	ñ	m	ń	ṇ	n	M
8.	jh	bh				Ṅ
9.			gh	ɖh	dh	S
10.	j	b	g	ɖ	d	Ś
11.	kh	ph	ch	ʈh	th	V
			c	ʈ	t	
12.	k	p				Y
13.			ś	ʂ	s	R
14.	h					L

अइउण्। क्रृल्क्।

a·i·uɳ | r̥·lk |

एओङ्। ऐऔच्।

e·oɳ | ai·auc |

हयवरट्। लण्।

hayavarat | lan |

ऋमडंणनम्। झ्वभञ्।

ñamanaŋnanam | jhabhañ |

घढधष्। जबगडदश्।

ghadhadhas | jabagadadas |

खफछठथचटतव्।

khaphachathathacatatav |

कपय्। शषसर्। हल्।

kapay | śaṣasar | hal |

Pratyāhāras

1.	a	i	u		N
2.			r	!	K
3.		e	o		N̄
4.		ai	au		C
5.	h	y	v	r	T

Pratyāhāras

1.	a	i	u		N
2.			r	l	K
3.		e	o		N
4.		ai	au		C
5.	h	y	v	r	T

aC

Pratyāhāras

1.	a	i	u			N
2.				r	l	K
3.		e	o			N̄
4.		ai	au			C
5.	h	y	v	r		T

aC = ⟨a, i, u, r, l, e, o, ai, au⟩

Analysis of *iko yanaci*: [iK] → [yN]/ [aC]

1.	a	i	u		N
2.				r !	K
3.		e	o		N
4.		ai	au		C
5.	h	y	v	r	T
6.				I	N

- *sūtra* 6.1.77: *iko yanaci* (इको यणचि)
- analysis: [ik]_{gen} [yan]_{nom} [ac]_{loc}
- [iK] → [yN]/ [aC]
- ⟨i, u, r, !⟩ → ⟨y, v, r, I⟩/ ⟨a, i, u, r, !, e, o, ai, au⟩
- dadhi + atra → dadhyatra

Our task

Pāṇini's method

- Unique method which is especially economical
- Method developed for a single language
- Testing of applicability to other languages

German as a test case

- Indoeuropean language with a smaller Sandhi-system
- No codified grammatical description
- 7 example processes of German

Phonological processes of German

final devoicing /hund/ 'dog' → [hʊnt]

⟨b, d, g, v, z, ʒ⟩ → ⟨p, t, k, f, s, ʃ⟩ / __ word boundary

umlaut [bal+ə] 'ball' (sg.) + plural → [belə]

⟨u:, ʊ, o:, ɔ, a:, a, aʊ⟩ → ⟨y:, ʏ, ø:, œ, ε:, ɛ, ɔɪ⟩

velar nasal assimilation /ankunft/ 'arrival' → [aŋkunft]

⟨n⟩ → ⟨ŋ⟩ / __ ⟨k, g⟩

labial nasal assimilation /anbaʊ̯/ 'outbuilding' → [ambəʊ̯]

⟨n⟩ → ⟨m⟩ / __ ⟨p, b, p̪, f, v⟩

glottal stop epenthesis /aɪ/ 'egg' → [ʔaɪ̯]

⟨ ⟩ → ⟨ʔ⟩ / word boundary __ vowel

vowel shortening /mo:næçɪ:/ 'monarchy' → [monaɛçɪ:]

⟨i:, y:, e:, ø:, u:, o:⟩ → ⟨i, y, e, ø, u, o⟩ / __ unstressed

palatal fricative assimilation /baç/ 'brook' → [bax]

⟨ç⟩ → ⟨x⟩ / ⟨a:, a, u:, ʊ, o:, ɔ, aʊ⟩ __

Set of 10 German sound classes that have to be described

devoicing input {b, d, g, v, z, ʒ}

devoicing output {p, t, k, f, s, ʃ}

umlaut input {u:, ʊ, o:, ɔ, a:, a, au̯}

umlaut output {y:, ʏ, ø:, œ, ε:, ε, ɔ̯}

nasal assimilation velar (right context) {k, g}

nasal assimilation labial (right context) {p, b, pf̩, f, v}

glottal stop epenthesis (right context)

{Y, ɛ, ə, ɪ, ε, œ, ɔ, ʊ, a, i, e, o, u, y, ø, a:, i:, ɔ:, u:, y:, ø:, e:, a:, ɔ:, au̯, ε:}

vowel shortening input {i:, y:, e:, ø:, u:, o:}

vowel shortening output {i, y, e, ø, u, o}

palatal fricative assimilation {a:, a, u:, ʊ, o:, ɔ, au̯}

Main theorem on *pratyāhārasūtras*

task

Given a set of sound classes find a list of the sounds in the style of Pāṇini's *Śivasūtras* (called *pratyāhārasūtras*) which provides a *pratyāhāra* for each sound class.

main theorem

A set of sound classes has *pratyāhārasūtras* in which no sound occurs more than once

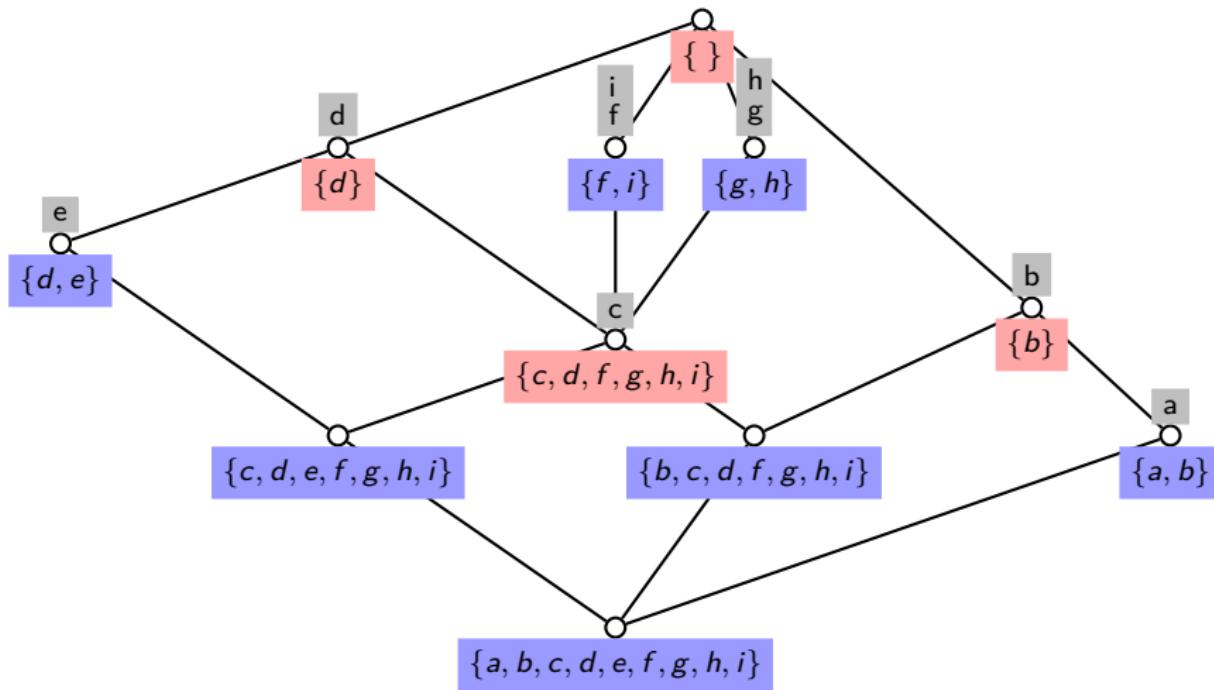
↔

the **concept lattice** of the set of sound classes is planar and each sound occurs on its *boundary*.

Petersen (2009): On the Construction of *Śivasūtra*-Alphabets. In Proc. of the 3rd Int. Sanskrit Comp. Ling. Symp.

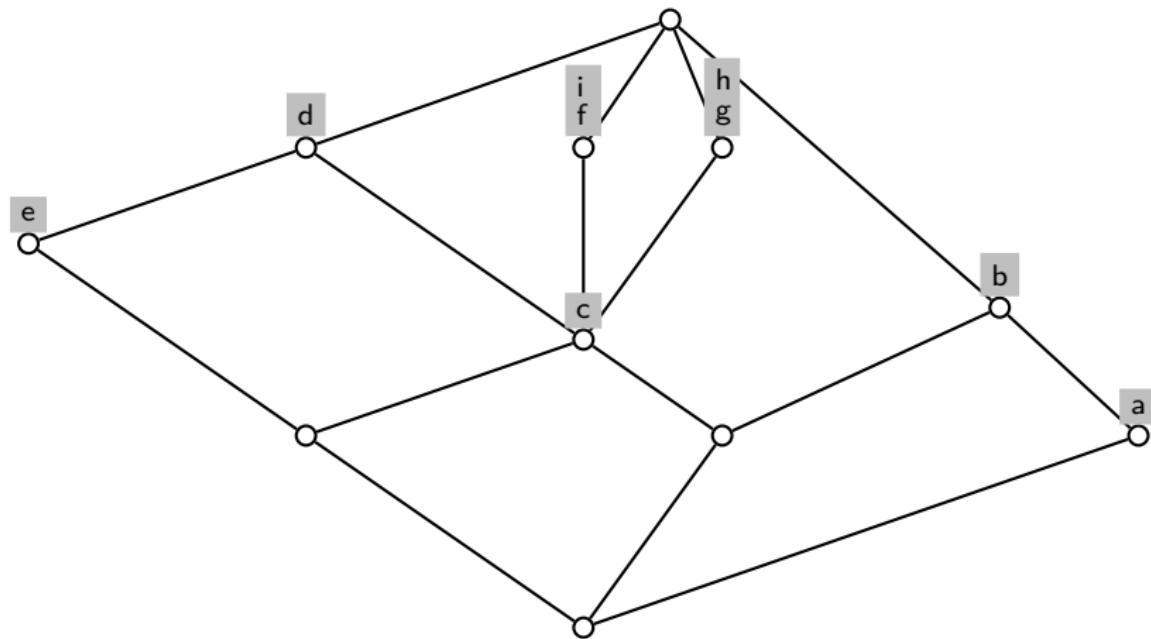
Example: concept lattice

$\{\{d, e\}, \{a, b\}, \{b, c, d, f, g, h, i\}, \{f, i\}, \{c, d, e, f, g, h, i\}, \{g, h\}\}$

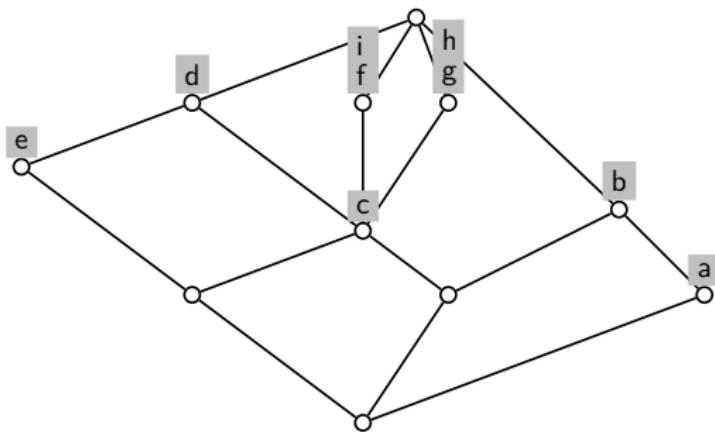


Example: concept lattice

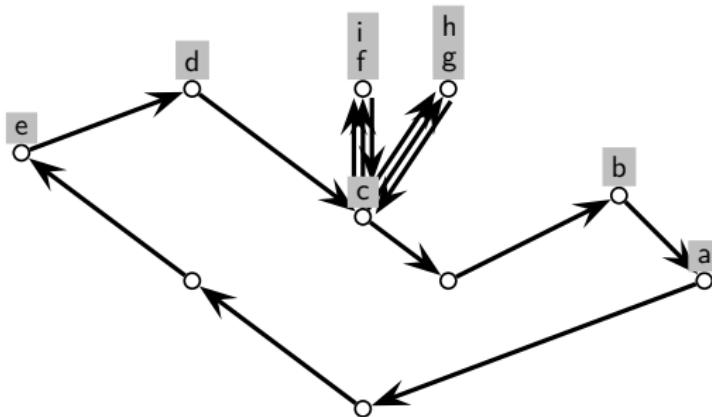
$\{\{d, e\}, \{a, b\}, \{b, c, d, f, g, h, i\}, \{f, i\}, \{c, d, e, f, g, h, i\}, \{g, h\}\}$



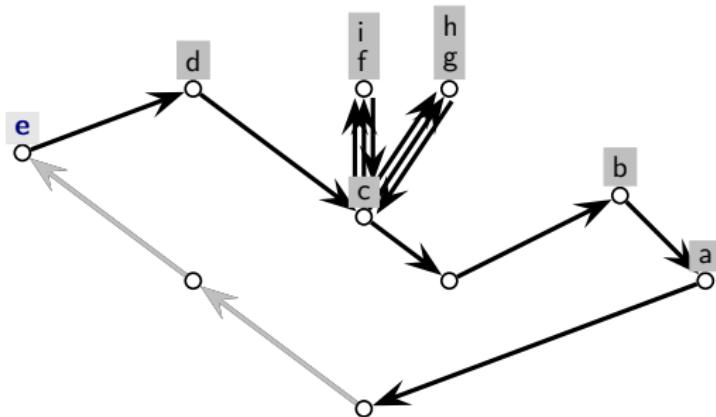
Pratyāhārasūtras with a minimal number of markers



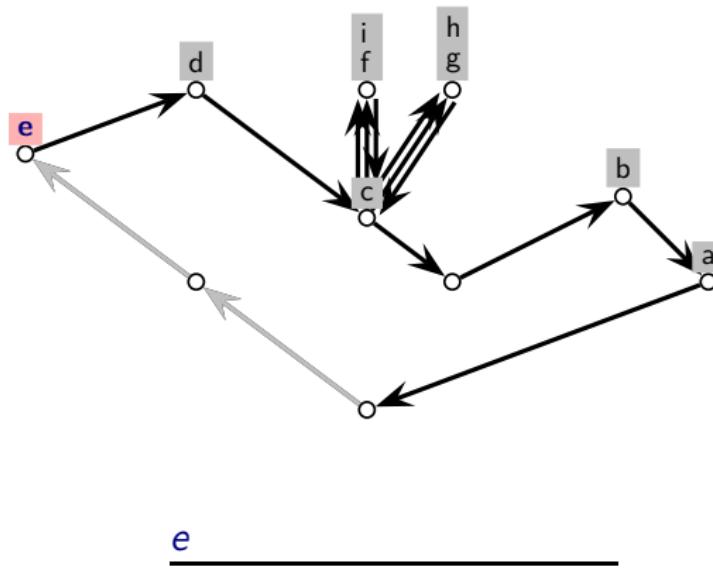
Pratyāhārasūtras with a minimal number of markers



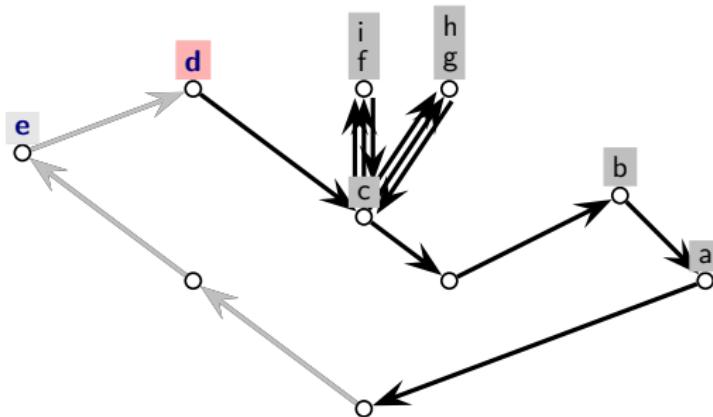
Pratyāhārasūtras with a minimal number of markers



Pratyāhārasūtras with a minimal number of markers

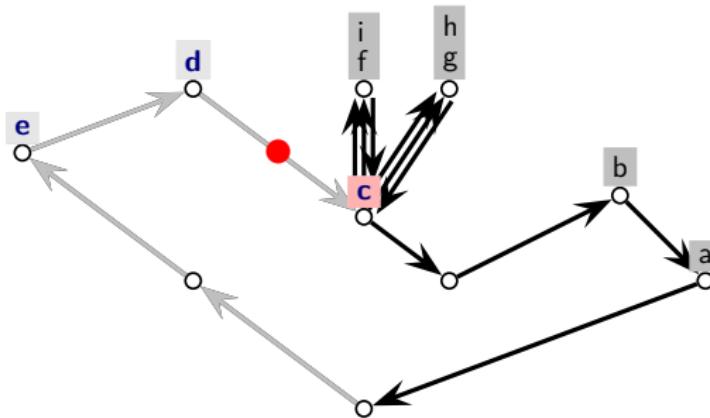


Pratyāhārasūtras with a minimal number of markers



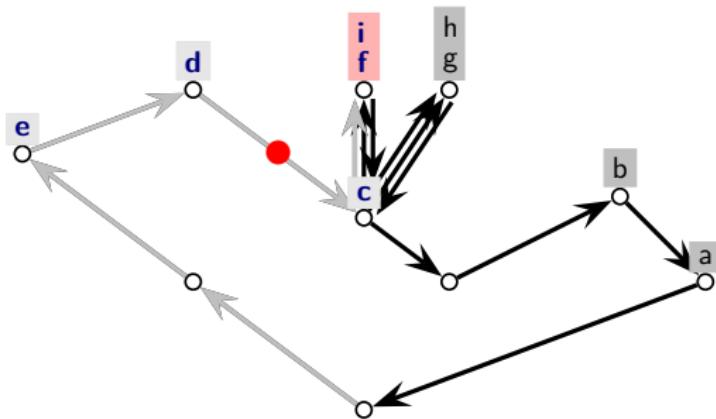
ed

Pratyāhārasūtras with a minimal number of markers

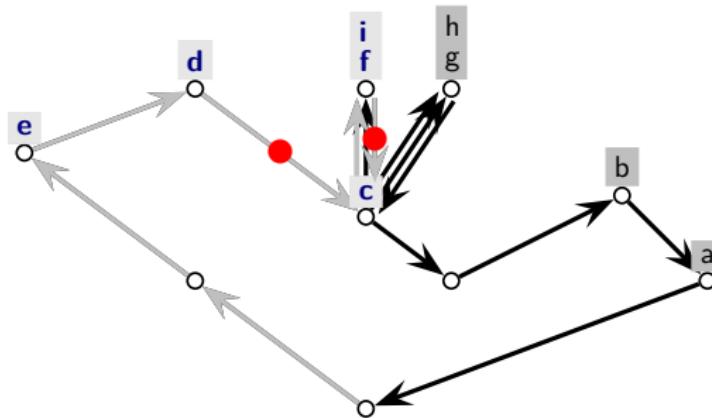


edM₁c

Pratyāhārasūtras with a minimal number of markers

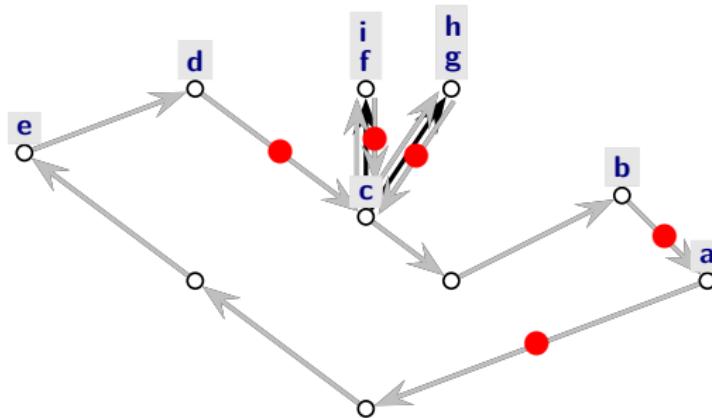


Pratyāhārasūtras with a minimal number of markers



edM_1cfiM_2

Pratyāhārasūtras with a minimal number of markers



edM₁cfiM₂ghM₃bM₄aM₅

Set of 10 German sound classes that have to be described

devoicing input {b, d, g, v, z, ʒ}

devoicing output {p, t, k, f, s, ʃ}

umlaut input {u:, ʊ, o:, ɔ, a:, a, au̯}

umlaut output {y:, ʏ, ø:, œ, ε:, ɛ, ɔ̯}

nasal assimilation velar (right context) {k, g}

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glottal stop epenthesis (right context)

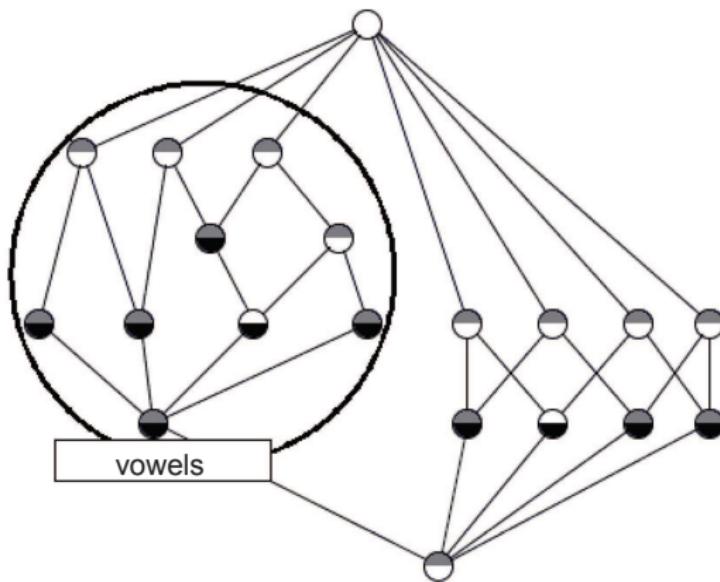
{Y, ɛ, ə, ɪ, ε, œ, ɔ, ʊ, a, i, e, o, u, y, ø, a:, i:, ɔ:, u:, y:, ø:, e:, a:, ɔ:, au̯, ε:}

vowel shortening input {i:, y:, e:, ø:, u:, o:}

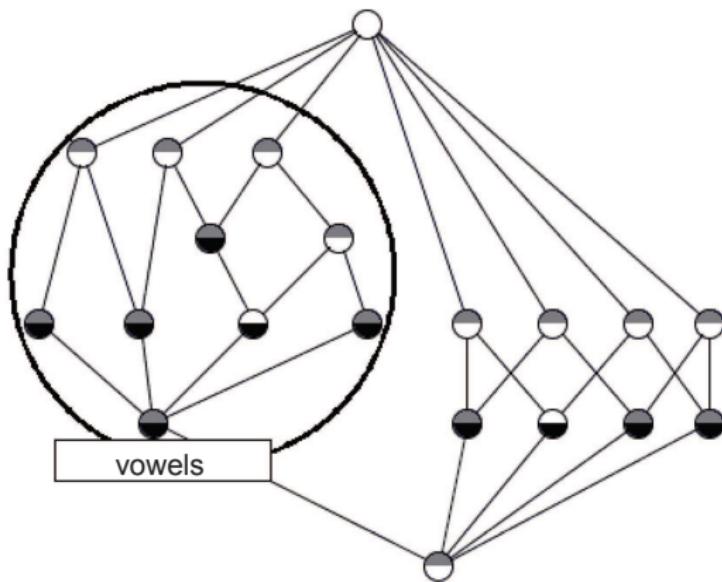
vowel shortening output {i, y, e, ø, u, o}

palatal fricative assimilation {a:, a, u:, ʊ, o:, ɔ, au̯}

German sound classes: concept lattice

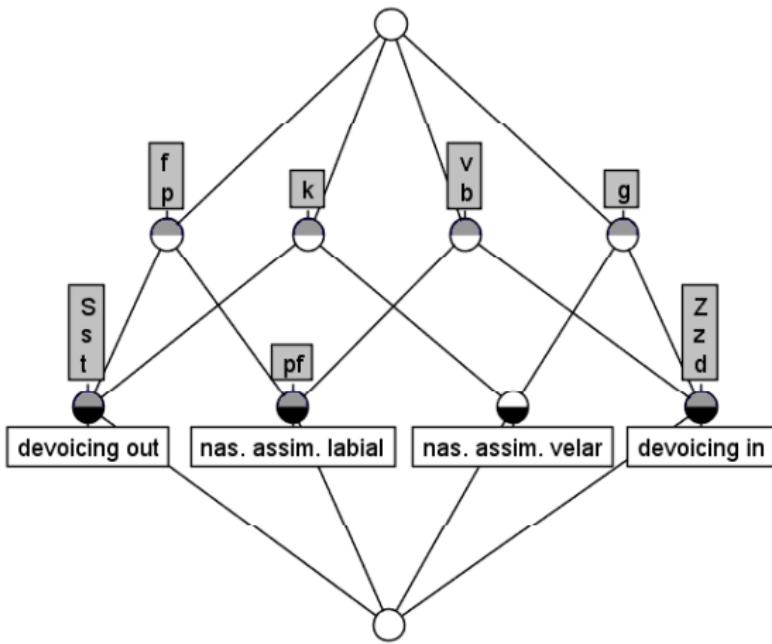


German sound classes: concept lattice

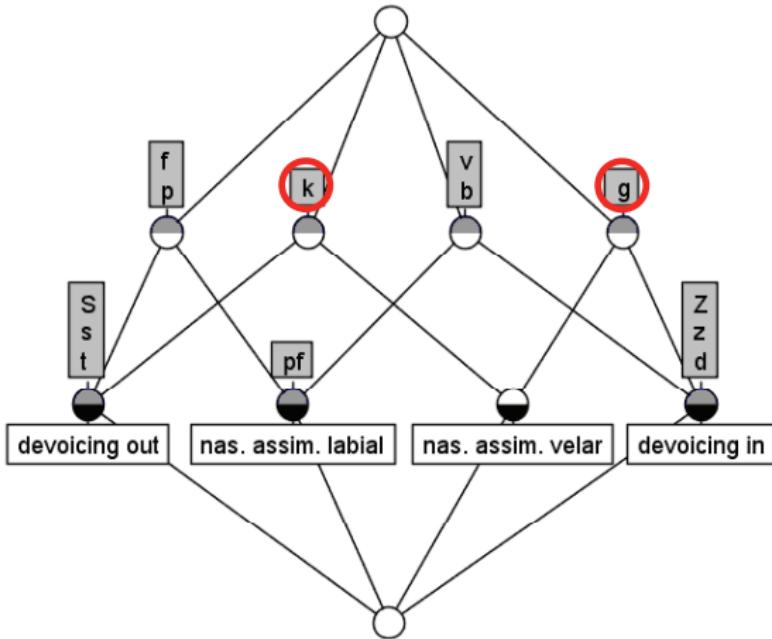


Vowels constitute a planar lattice

Consonants constitute a non-planar lattice

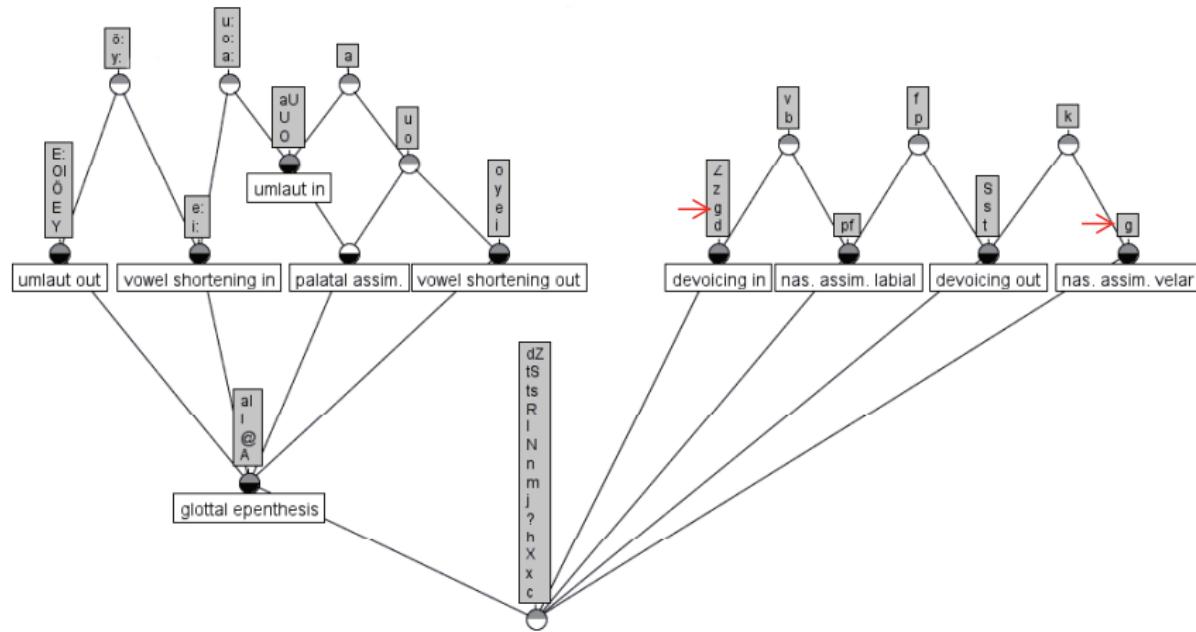


Consonants constitute a non-planar lattice



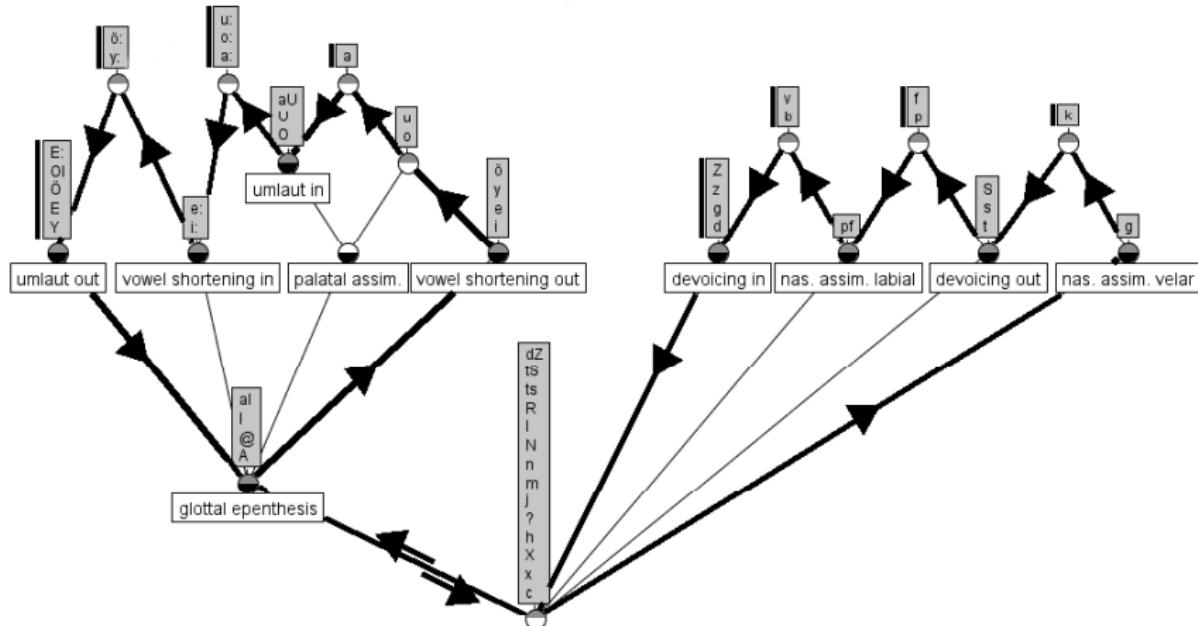
Duplication of a consonant necessary!

Proposed *pratyāhārasūtras* for German



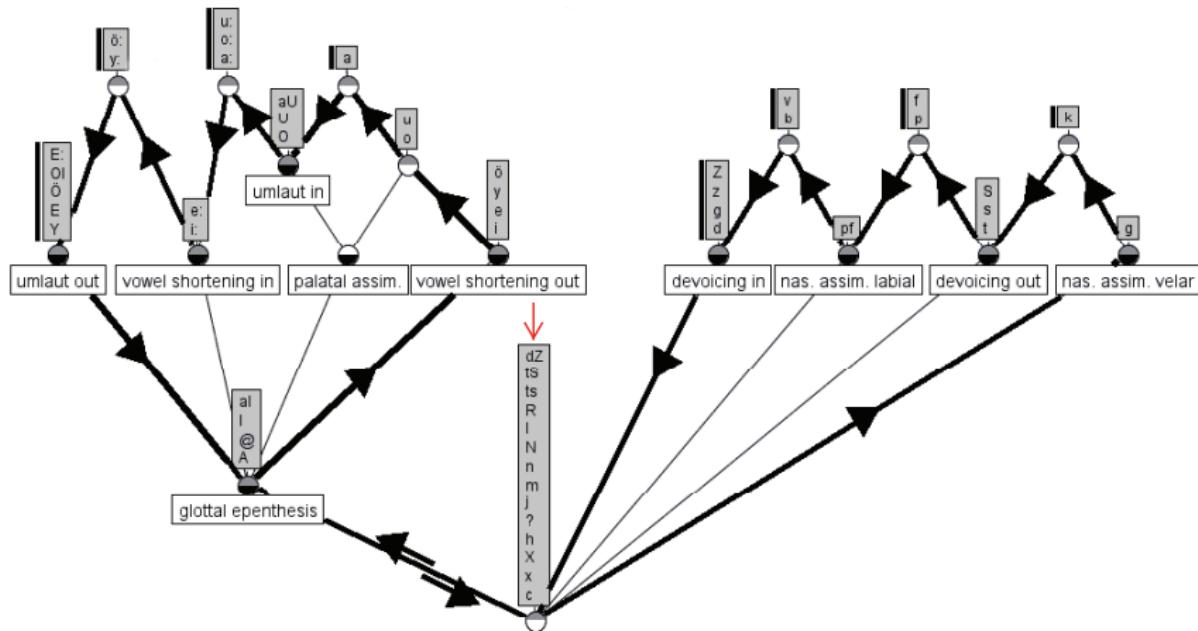
$\widehat{d}_3 \widehat{t} \widehat{s} \text{ b l } \text{ŋ} \text{ n } \text{m } \text{j } ? \text{ h } \text{ç } \text{x } \text{g } \text{k } M_1 \text{ t } \text{s } \text{ʃ } \text{f } \text{p } M_2 \widehat{\text{pf}} \text{ b } \text{v } M_3 \text{ z } \text{d } \text{g } M_4$
 $\text{ə } \text{æ } \text{i } \text{ɪ } \text{aɪ } \text{ø } \text{y } \text{e } \text{i } \text{u } \text{o } \text{a } M_5 \text{ v } \text{ɔ } \text{aʊ } \text{a: } \text{o: } \text{u: } M_6 \text{ i: } \text{ɛx } \text{y: } \text{ɸ: } M_7 \text{ ε: } \text{ɔɪ } \text{œ } \text{y } \text{ɛ } M_8$

Proposed *pratyāhārasūtras* for German



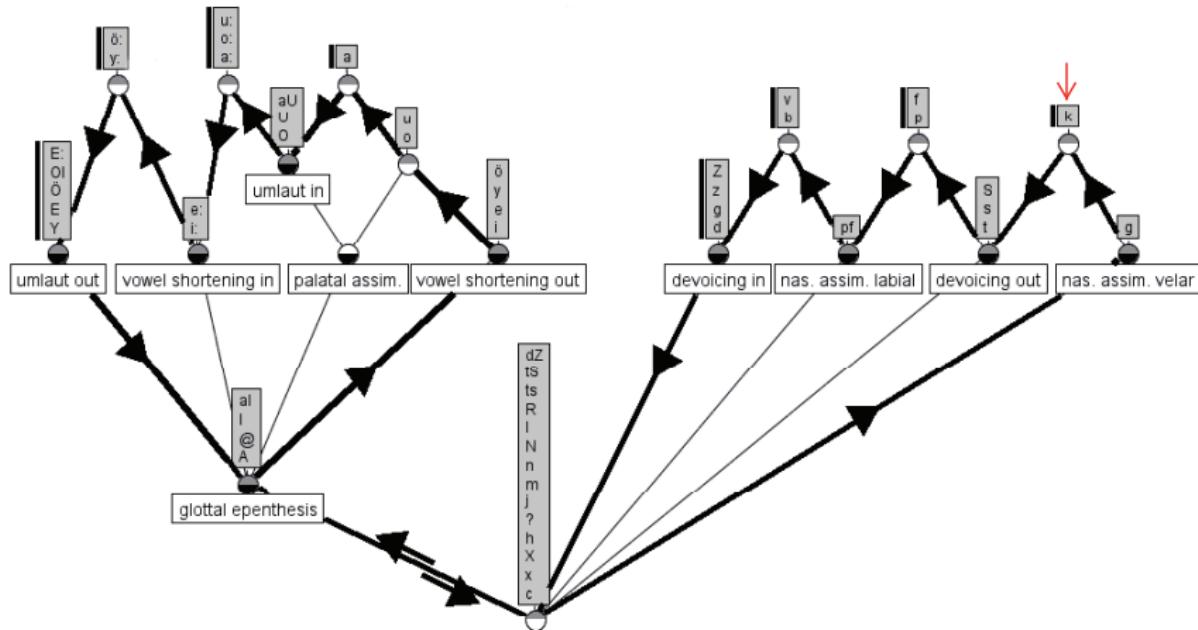
$\widehat{d}_3 \widehat{t} \widehat{s} \widehat{b} l \widehat{y} n m j ? h \widehat{ç} x g k M_1 t s \widehat{s} f p M_2 \widehat{pf} b v M_3 \widehat{z} d g M_4$
 $e a i \widehat{ai} \emptyset y e i u o a M_5 \widehat{u} \circ a \widehat{ø} a: o: u: M_6 i: e x y: \emptyset: M_7 \varepsilon: \circ \widehat{i} \circ e y \varepsilon M_8$

Proposed *pratyāhārasūtras* for German



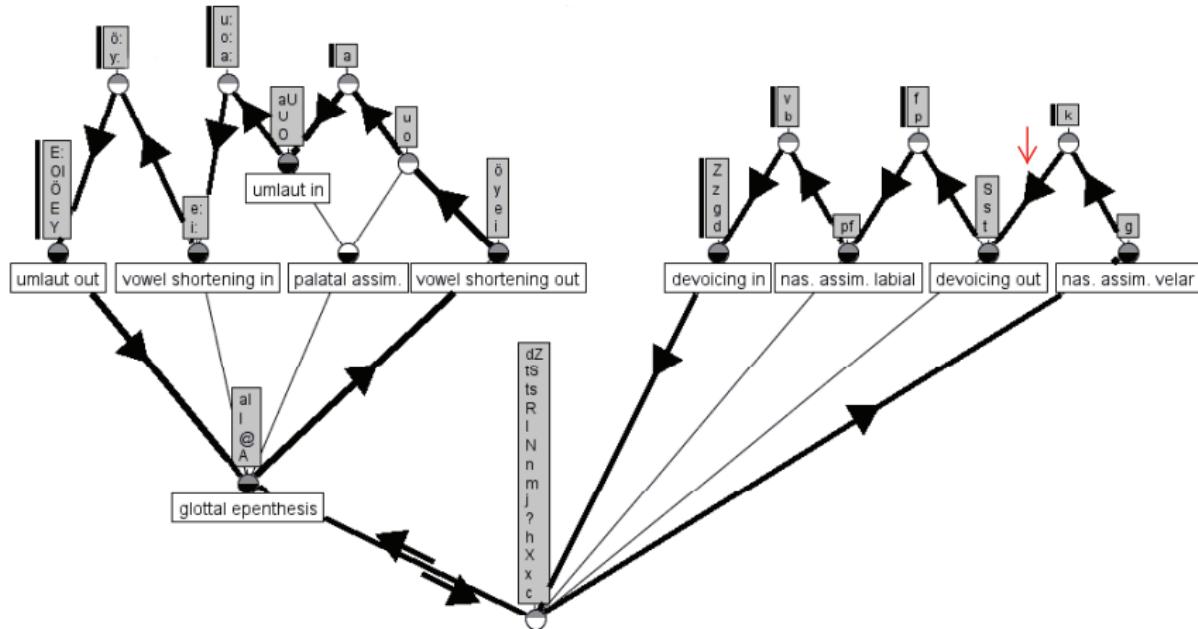
dʒ tʃ ts ʌ l ʃ n m j ? h ç x g k M₁ t s ſ f p M₂ p̪f b v M₃ ʒ z d g M₄
ə e i aɪ əʊ y e i u o a M₅ ʊ ɔ aʊ a: o: u: M₆ i: e: y: ə: M₇ ε: ɔɪ œ y ε M₈

Proposed *pratyāhārasūtras* for German



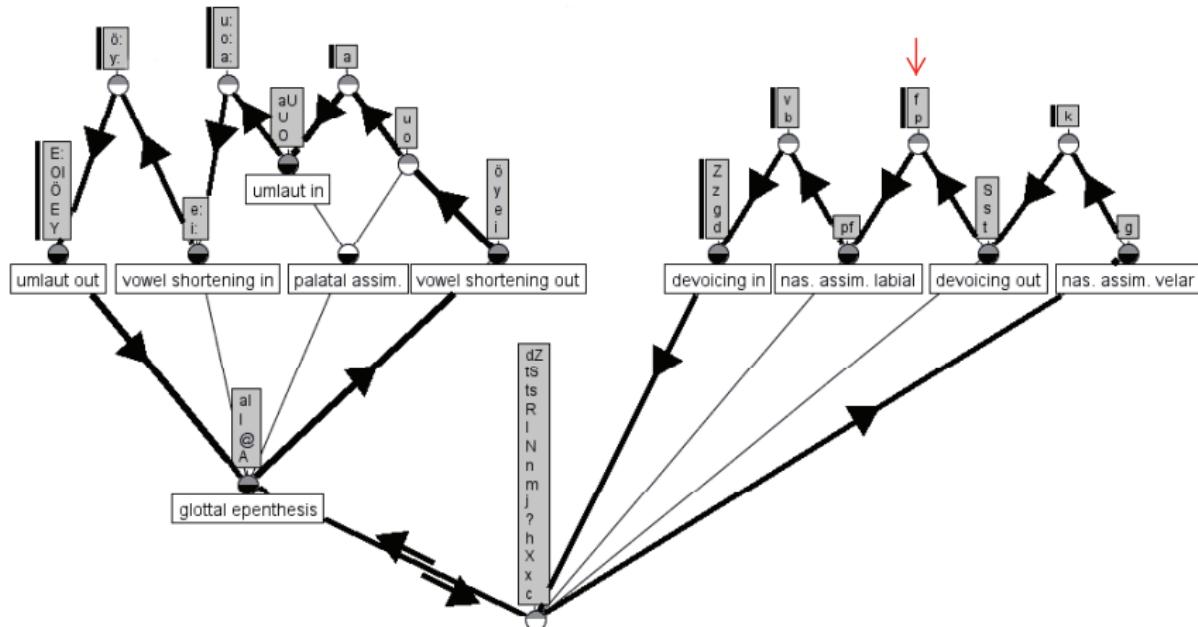
$\widehat{d}_3 \widehat{t} \widehat{f} \widehat{ts} \widehat{b} \widehat{l} \widehat{y} \widehat{n} \widehat{m} \widehat{j} \widehat{?} \widehat{h} \widehat{\zeta} \widehat{x} \widehat{g} \widehat{k} M_1 \widehat{t} \widehat{s} \widehat{\int} \widehat{f} \widehat{p} M_2 \widehat{pf} \widehat{b} \widehat{v} M_3 \widehat{z} \widehat{d} \widehat{g} M_4$
 e a i ai ø y e i u o a M₅ u o a y a: o: u: M₆ i: ex y: ø: M₇ ε: œ: y ε M₈

Proposed *pratyāhārasūtras* for German



$\widehat{d}_3 \widehat{t} \widehat{f} \widehat{ts} \widehat{b} \widehat{l} \widehat{y} \widehat{n} \widehat{m} \widehat{j} \widehat{?} \widehat{h} \widehat{\zeta} \widehat{x} \widehat{g} \widehat{k} M_1 \widehat{t} \widehat{s} \widehat{\int} \widehat{f} \widehat{p} M_2 \widehat{pf} \widehat{b} \widehat{v} M_3 \widehat{z} \widehat{d} \widehat{g} M_4$
 e a i ai ø y e i u o a M_5 u o a ø a: o: u: M_6 i: ex y: ø: M_7 ε: œi œ y ε M_8

Proposed *pratyāhārasūtras* for German



$\widehat{d_3} \widehat{t\chi} \widehat{t\hat{\epsilon}} \widehat{b} \widehat{l} \widehat{\chi} \widehat{n} \widehat{m} \widehat{j} \widehat{?} \widehat{h} \widehat{\zeta} \widehat{x} \widehat{g} \widehat{k} M_1 \widehat{t} \widehat{s} \widehat{\mathfrak{f}} \widehat{f} \widehat{p} M_2 \widehat{pf} \widehat{b} \widehat{v} M_3 \widehat{\mathfrak{z}} \widehat{z} \widehat{d} \widehat{g} M_4$
 $\widehat{\mathfrak{e}} \widehat{\mathfrak{æ}} \widehat{i} \widehat{\mathfrak{ɪ}} \widehat{\mathfrak{aɪ}} \widehat{\mathfrak{y}} \widehat{\mathfrak{e}} \widehat{\mathfrak{i}} \widehat{\mathfrak{u}} \widehat{\mathfrak{o}} \widehat{a} M_5 \widehat{\mathfrak{ʊ}} \widehat{\mathfrak{ɔ}} \widehat{\mathfrak{aʊ}} \widehat{a:} \widehat{o:} \widehat{u:} M_6 \widehat{i:} \widehat{e:} \widehat{y:} \widehat{\mathfrak{ɸ}:} M_7 \widehat{\mathfrak{ɛ:}} \widehat{\mathfrak{ɔɪ}} \widehat{\mathfrak{œ}} \widehat{Y} \widehat{\mathfrak{ε:}} M_8$

Resulting *pratyāhāras*

d̄ʒ̄ tʃ̄ ts̄ b̄ l̄ ɻ̄ n̄ m̄ j̄ ? h̄ ç̄ x̄ ḡ k̄ M₁ t̄ s̄ ſ̄ f̄ p̄ M₂ p̄f̄ b̄ v̄ M₃
 ʒ̄ z̄ d̄ ḡ M₄ ə̄ ē ī āī ɸ̄ ȳ ē ī ū ō ā M₅ ʊ̄ ɔ̄ āȳ ā: ō: ū: M₆ ī: ē: ȳ: ɸ̄: M₇
 ε̄ ɔ̄ī œ̄ ȳ ε̄ M₈

- bM₄ Input to final devoicing
- kM₂ Output to final devoicing
- gM₁ Input to velar nasal assimilation
- fM₃ Input to labial nasal assimilation
- uM₆ Context of palatal fricative assimilation
- aM₆ Input to umlaut
- y:M₈ Output to umlaut
- a:M₇ Input to vowel shortening
- ɸM₅ Output to vowel shortening
- əM₈ Context of glottal epenthesis

Resulting *pratyāhāras*

dʒ tʃ ts ɹ l ɳ n m j ɿ h ç x g k M₁ t sʃ f p M₂ ɸ b v M₃
 ʂ z d g M₄ ə ɐ i ɐ̂ y e ɪ u o a M₅ ʊ ɔ ɐ̄ a ɔ: u: M₆ i: e: y: ɸ: M₇
 ε: ɪ ɔ: ʊ ɛ y ɛ M₈

- bM_4 Input to final devoicing ⟨b v ʒ z d ɡ⟩
 - kM_2 Output to final devoicing ⟨k t s ʃ f p⟩
 - gM_1 Input to velar nasal assimilation
 - fM_3 Input to labial nasal assimilation
 - uM_6 Context of palatal fricative assimilation
 - aM_6 Input to umlaut
 - $y:M_8$ Output to umlaut
 - $a:M_7$ Input to vowel shortening
 - $\emptyset M_5$ Output to vowel shortening
 - $\emptyset M_8$ Context of glottal epenthesis

Phonological processes in *pratyāhāra* notation

$\widehat{d_3} \widehat{t\text{ʃ}} \widehat{\text{ts}}$ b l ŋ n m j ? h ç x g k M_1 t s ſ f p M_2 $\widehat{\text{pf}}$ b v M_3
 z z d g M_4 e e i a ɪ \emptyset y e i u o a M_5 u o a ʊ a: o: u: M_6 i: e: y: \emptyset : M_7
 ε: o ɪ oe y ε M_8

- $bM_4 \rightarrow kM_2 / _ \text{ word boundary}$ final devoicing
- $/n/ \rightarrow [\text{ŋ}] / _ gM_1$ velar nasal assimilation
- $/n/ \rightarrow [m] / _ fM_3$ labial nasal assimilation
- $\{ \} \rightarrow [?] / \text{ word boundary } _ \emptyset M_8$ glottal stop epenthesis
- $a:M_7 \rightarrow \emptyset M_5 / _ \text{unstressed}$ vowel shortening
- $/\text{ç}/ \rightarrow [x] / uM_6 _$ palatal fricative assimilation
- $aM_6 \rightarrow y:M_8$ umlaut

Summary & outlook

- The *pratyāhāra* method is applicable to the description of the sound system of German
- Our sample of German phonological processes is rather small
- Further languages (e.g. non-Indoeuropean, or with larger Sandhi-systems) have to be investigated